

B.TECH. DEGREE EXAMINATION, DECEMBER 2012**Third Semester**

Branch : Common to all Branches except CS and IT

EN 010 301-A—ENGINEERING MATHEMATICS—II

(CE, ME EE, AU, AN, EC, AI, EI, IC, PE AND PO)

[New Scheme—Regular/Improvement/Supplementary]

Time : Three Hours

Maximum : 100 Marks

Part A*Answer all questions.**Each question carries 3 marks.*

1. Evaluate $\text{grad} \left(\frac{1}{r} \right)$ where $r = |\vec{r}|$ and $\vec{r} = x\vec{i} + y\vec{j} + z\vec{k}$.
2. If R is a region bounded by a simple closed curve C, then using Green's theorem show that the area of R is given by $\frac{1}{2} \oint_C [x dy - y dx]$.
3. Prove that $\Delta \log f(x) = \log \{1 + \Delta f(x)\}$.
4. What is numerical differentiation ? Explain.
5. Find $Z\{\sin(3n+5)\}$.

(5 × 3 = 15 marks)

Part B*Answer all questions.**Each question carries 5 marks.*

6. If $\vec{f} = xyz\vec{i} + 3x^2y\vec{j} + (xz^2 - y^2z)\vec{k}$ find $\text{div } \vec{f}$ and $\text{curl } \vec{f}$ at (1, 2, 3).
7. If $\vec{F} = (3x^2 + 6y)\vec{i} - 14yz\vec{j} + 20xz^2\vec{k}$ evaluate $\int_C \vec{F} \cdot d\vec{r}$ from (0, 0, 0) to (1, 1, 1) along the path $x = t, y = t^2$ and $z = t^3$.
8. Prove that : (a) $E^{\frac{1}{2}} - \frac{1}{2}f - \mu = 0$ and (b) $\Delta = \frac{1}{2}f^2 + f\sqrt{1 + \frac{f^2}{4}}$.

Turn over